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## **CLAIMS**

Having thus described our invention, what we claim as new and desire to secure by Letters Patent is as follows:

1. A method for making prioritized recommendations to a customer in the process of filling a market basket for purchase on an Internet commerce site, the method comprising the steps of:

generating a matrix of training data;

considering preferences based on associative and renewal buying history from the training data; and

making a prioritized recommendation of items so as to maximize the likelihood that the customer will add to the market basket those items with higher priorities.

- 2. The method of claim 1 wherein the two preferences are estimated separately from the training data and combined in proper proportions to obtain an overall preference for item not yet in the market basket.
- 3. A method for making prioritized recommendations to a customer in the process of filling a market basket for purchase on an Internet commerce site, the method comprising the steps of:

collecting statistics from training data;

precomputing model parameters from the collected statistics; and recommending ordering for a given partial market basket based on the precomputed model parameters.

4. The method of claim 3, wherein the step of collecting statistics comprises the steps of:

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- (a) for each item j, obtaining  $n_j$  a number of baskets with item j purchased;
- 4 (b) for each item j, obtaining  $n_j$  a number of baskets with j being a sole item purchased;
  - (c) for each pair of items i and j, obtaining a number of market baskets  $n_{ji}$  with items j and i purchased together; and
- 8 (d) for each pair of items i and j, obtaining a number of market baskets 9  $n_{ji}$  with items i and j being the only two items purchased.
  - 5. The method of claim 4, wherein the step of precomputing model parameters comprises the steps of:
    - (a) computing P(renewal) =  $\frac{\sum_{k} n_{k}'}{\sum_{k} n_{k}}$
  - (b) for each item j, computing  $P(j) = \frac{n_j}{\sum_k n_k}$ ;
- 5 (c) for each item j,
- 6 computing  $\mathbf{P}(\text{renewal} \mid j) = \frac{n_j'}{n_j} + \mathbf{P}(\text{renewal}) \left(1 \frac{n_j'}{n_j}\right)$ ;
- 7 (d) for each item j, computing
- 8  $\mathbf{P}'(j \mid \text{renewal}) = \mathbf{P}(\text{renewal} \mid j) \times \frac{\mathbf{P}(j)}{\mathbf{P}(\text{renewal})};$
- 9 (e) for each pair of items i and j with  $n_{ij} \neq 0$ , computing

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$$\mathbb{P}(j \mid i) = \frac{n_{j|}}{\sum_{k} n_{ki}};$$

for each pair of items i and j with  $n_{ij} \neq 0$ , computing 11

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$$\mathbb{P}(\text{renewal} \mid j,i) = \frac{n_{ji}'}{n_{ji}} + \mathbb{P}(\text{renewal}) \left(1 - \frac{n_{ji}'}{n_{ji}}\right)$$
; and

(g) for each pair of items  $\bar{i}$  and j with  $n_{ij} \neq 0$ , computing 13

$$\mathbb{P}'(j \mid \text{asso},i) = \mathbb{P}(j \mid i) \times \frac{(1 - \mathbb{P}(\text{renewal} \mid j,i))}{(1 - \mathbb{P}(\text{renewal} \mid i))}.$$

- 6. The method of claim 5, wherein given a partial basket  $\mathbb{B} = \{i_1, i_2, \dots, i_k\}$ and  $\overline{B}$  is a complementary set of items not in B, the step of recommending ordering for a given partial market basket comprises the steps of:
  - (a) if B is empty, sorting items in order of decreasing  $P(j \mid \text{renewal})$  and returning this as an item preference ordering;
  - (b) if B is non-empty, then
    - computing  $\mathbb{P}(\text{renewal} \mid \mathbb{B}) = \min_{i_k \in \mathbb{B}} \mathbb{P}(\text{renewal} \mid i_k)$ ; (i)
    - compute a normalization factor  $\sum_{k \in \overline{B}} \mathbb{P}'(k \mid \text{renewal})$ ; (ii)
  - for each item  $j \in \overline{\mathbb{B}}$ , computing (iii)

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$$\mathbb{P}(j \mid \text{renewal}) = \frac{\mathbb{P}'(j \mid \text{renewal})}{\sum_{k \in \overline{\mathbf{B}}} \mathbb{P}'(k \mid \text{renewal})};$$

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11	(iv)	computing a normalization factor	$\sum_{k\in\overline{\mathbf{B}}}\mathbf{P}'(j\mid \mathrm{asso},\mathbf{B})\;;$
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12 (v) for each item 
$$j \in \overline{\mathbf{B}}$$
, computing

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$$\mathbf{P}'(j \mid \mathrm{asso}, \mathbf{B}) = \max_{i_k \in \mathbf{B}} \mathbf{P}(j \mid \mathrm{asso}, i_k) ;$$

(vi) for each item 
$$j \in \overline{\mathbf{B}}$$
, computing

and

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$$\mathbf{P}(j \mid \mathrm{asso},\mathbf{B}) = \frac{\mathbf{P}'(j \mid \mathrm{asso},\mathbf{B})}{\sum_{k \in \overline{\mathbf{B}}} \mathbf{P}'(k \mid \mathrm{asso},\mathbf{B})};$$

16 (vii) for each item 
$$j \in \overline{\mathbf{B}}$$
, computing

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$$\mathbf{P}(j|\mathbf{B}) = \mathbf{P}(j \mid \text{asso}, \mathbf{B}) \mathbf{P}(\text{asso} \mid \mathbf{B}) + \mathbf{P}(j \mid \text{renewal}, \mathbf{B}) \mathbf{P}(\text{renewal} \mid \mathbf{B});$$

(viii) sorting items in order of decreasing P(j | B) and returning this as an item preference ordering.

7. The method of claim 6, wherein the step of sorting comprises the step of using a final probability obtained for each item, P(j | B), of a customer buying the item to maximize profit by recommendation.

8. The method of claim 7, wherein the step of using a final probability of an item to maximize profit comprises the steps of:

3 assigning a profit amount, \$, to each item;

4 computing P(j | B), for each item; and

ranking recommendations based on the computation of P(j | B) for

6 each item.